



Examiner : Dr. Mustafa M. Shiple
 Subject: Autonomous Multiagent Systems (AI 314)
 Score: 10 Marks

Term: Spring 2023
 Exam Time:60 min

Instructions:

- Use the space provided to write your answers.
- Ask in case of doubt.

ANSWER THE FOLLOWING QUESTIONS:

1. Fill in the spaces [5 marks]
- Genetic Algorithms (GA) use principles of natural evolution. There are five important features of GA
 - Mutation is a technique that
 - IF environment is nondeterministic, the agent doesn't know what isstate after
 - In games theory, Zero-sum means
 - Monte Carlo methods rely onsampling to obtain numerical results.

Solution:

- Initial Population, Fitness Function, Selection, Crossover, Mutation.
- flips a randomly selected gene in a chromosome.
- next , taking an action
- one players loss is the others gain.
- repeated random .

2. Suppose a genetic algorithm uses chromosomes of the form $x = abcdefgh$ with a fixed length of eight genes. Each gene can be any digit between 0 and 9. Let the fitness of individual x be calculated as:

$$f(x) = (a + b)(c + d) + (e + f)(g + h),$$

and let the initial population consist of four individuals with the following chromosomes:

- $x_1 = 2\ 3\ 9\ 2\ 1\ 2\ 8\ 5$
- $x_2 = 6\ 5\ 4\ 1\ 3\ 5\ 3\ 2$
- $x_3 = 8\ 7\ 1\ 2\ 6\ 6\ 0\ 1$
- $x_4 = 4\ 1\ 8\ 5\ 2\ 0\ 9\ 4$

if individual operations are defined as:-

- Cross operation: a onepoint crossover at the middle point.
 - Mutation operation: third digit only in last generated offspring.
 - Roulette wheel : when it rotated the outcome will be $\{3, 1, 4, 2, 1, 2, 4, 3, 4, 1, 4, 5, 1, 3, 2, 6, 4, 2, 3, 5\}$
- (a) Perform two complete cycles of genetic algorithm, each generation consists of **6 chromosomes** .

[Total Marks is 10]

Solution:

$$f(x_1) = (2 + 3)(9 + 2) + (1 + 2)(8 + 5) = -16$$

$$f(x_2) = (6 + 5)(4 + 1) + (3 + 5)(3 + 2) = 9$$

$$f(x_3) = (8 + 7)(1 + 2) + (6 + 6)(0 + 1) = 23$$

$$f(x_4) = (4 + 1)(8 + 5) + (2 + 0)(9 + 4) = -19$$

order: x3-x2-x1-x4

Due to roulette wheel and cross operation the pairs are :

$$(x_1, x_3) = x_5 = 23926601 = (2 + 3)(9 + 2) + (6 + 6)(0 + 1) = 5$$

$$(x_4, x_2) = x_6 = 41853532 = (4 + 1)(8 + 5) + (3 + 5)(3 + 2) = -5$$

$$(x_3, x_2) = x_7 = 87123532 = (8 + 7)(1 + 2) + (3 + 5)(3 + 2) = 15$$

$$(x_1, x_4) = x_8 = 23922094 = (2 + 3)(9 + 2) + (4 + 1)(8 + 5) = -17$$

$$(x_4, x_1) = x_9 = 41851285 = (4 + 1)(8 + 5) + (1 + 2)(8 + 5) = -18$$

$$x_3 = 87126601 = 23$$

Mutation : $x_9 = 4\ 1\ 1\ 5\ 1\ 2\ 8\ 5 = -11$

first generation :

$$1x_3 = 87126601 = 23$$

$$2x_7 = 87123532 = 15$$

$$3x_5 = 23926601 = 5$$

$$4x_6 = 41853532 = -5$$

$$5x_9 = 41851285 = -11$$

$$6x_8 = 23922094 = -18$$

Due to roulette wheel and cross operation the pairs are :

$$(x_6, x_9) = x_{10} = 41851285 = (2 + 3)(9 + 2) + (6 + 6)(0 + 1) = -17$$

$$(x_3, x_5) = x_{11} = 87126601 = (4 + 1)(8 + 5) + (3 + 5)(3 + 2) = 23$$

$$(x_7, x_8) = x_{12} = 87122094 = (8 + 7)(1 + 2) + (3 + 5)(3 + 2) = 1$$

$$(x_6, x_7) = x_{13} = 41853532 = (2 + 3)(9 + 2) + (4 + 1)(8 + 5) = -5$$

$$(x_3, x_9) = x_{14} = 87121285 = (4 + 1)(8 + 5) + (1 + 2)(8 + 5) = 2$$

$$x_3 = 87126601 = 23$$

Mutation : $x_{14} = 87021285 = 3$ Second offspring :

$$x_{10} = 41851285$$

$$x_{11} = 87126601$$

$$x_{12} = 87122094$$

$$x_{13} = 41853532$$

$$x_{14} = 87121285$$

$$x_3 = 87126601 = 23$$