

SEARCH IN COMPLEX ENVIRONMENTS II

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Evolutionary algorithms()

Developed: USA in the 1970's

Early names: J. Holland, K. DeJong, D. Goldberg

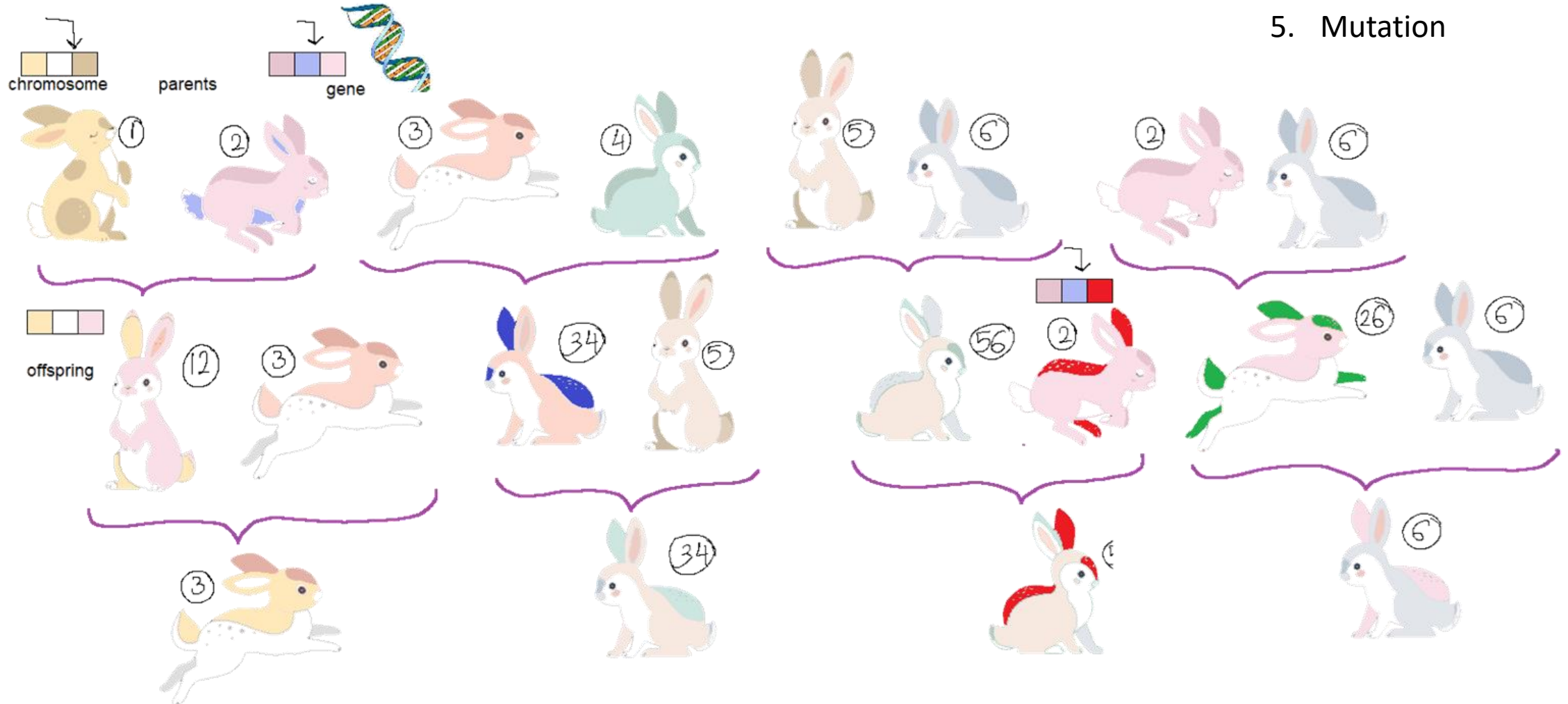
Genetic Algorithms

How is a population with increasing fitness generated?

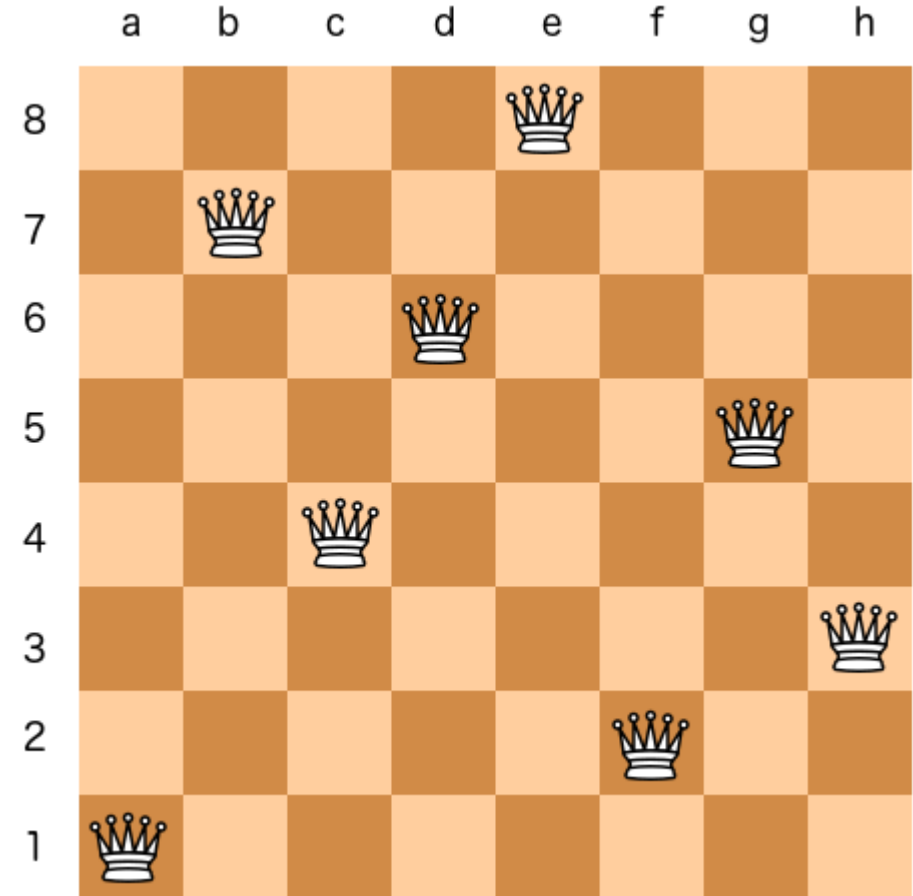
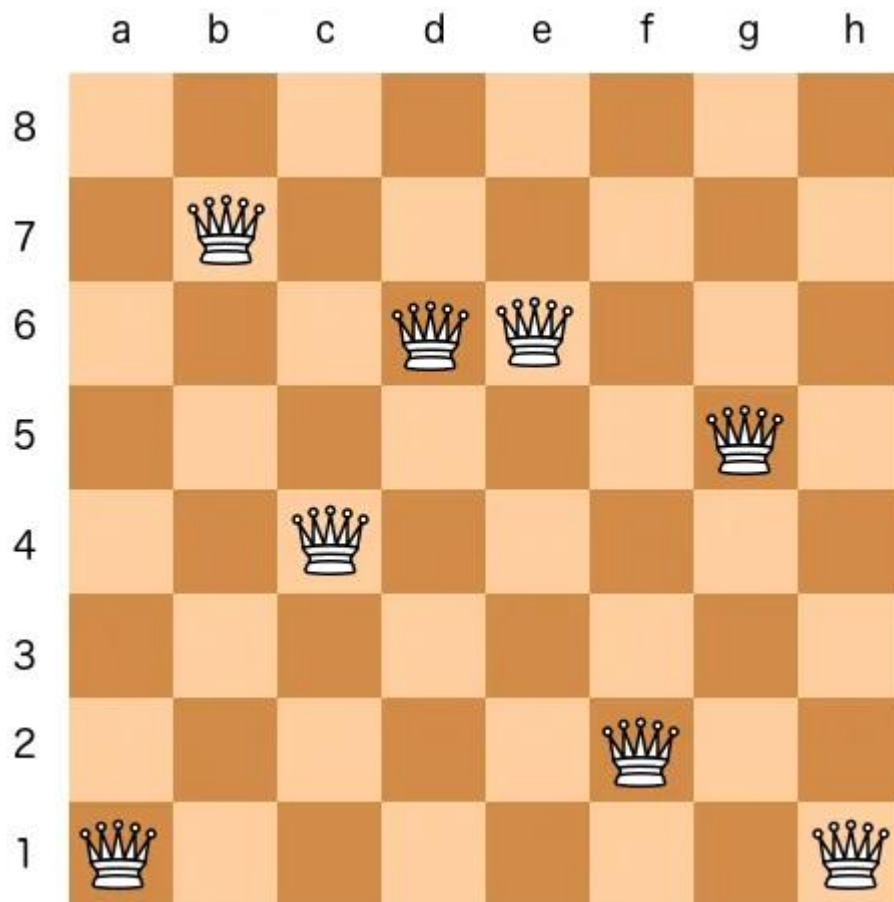
- Let us consider a population of rabbits. Some rabbits are faster than others, and we may say that these rabbits possess superior fitness, because they have a greater chance of avoiding foxes, surviving and then breeding.
- If two parents have superior fitness, there is a good chance that a combination of their genes will produce an offspring with even higher fitness. Over time the entire population of rabbits becomes faster to meet their environmental challenges in the face of foxes.

How is a population with increasing fitness generated?

1. Initial Population
2. Fitness Function
3. Selection
4. Crossover
5. Mutation



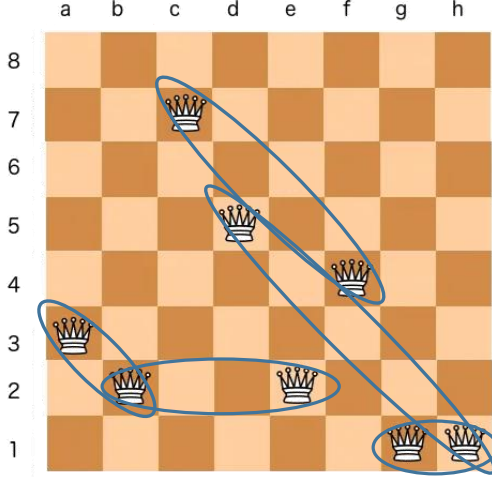
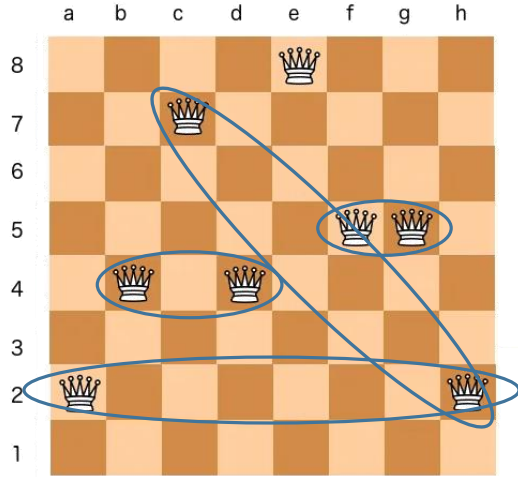
Case Study : 8 Queen problem



Representation (numeric)

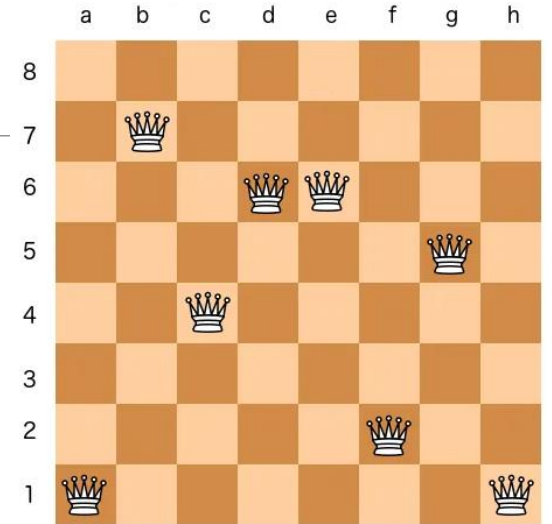
24748552

non attacked pair=24



32752411

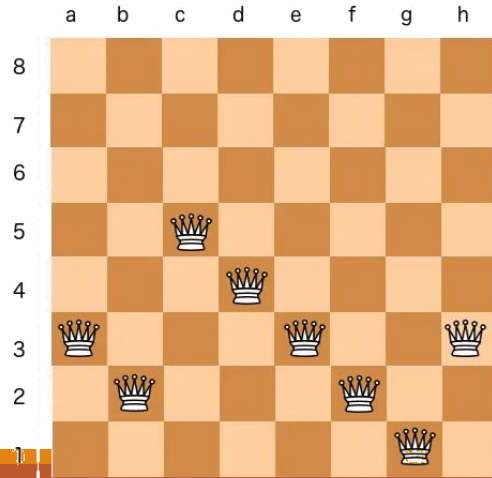
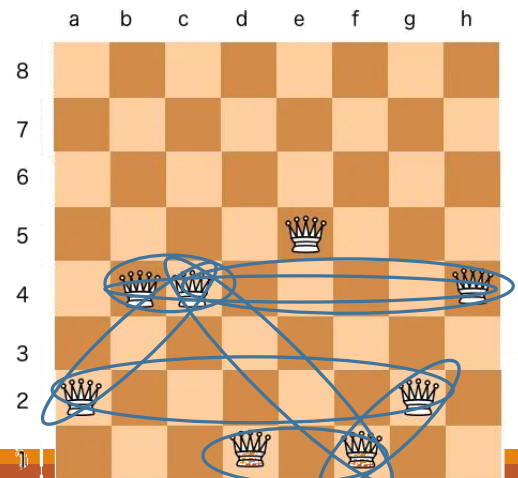
non attacked pair=23



[1,7,4,6,6,2,5,1]

24415124

non attacked pair=20



32543213

non attacked pair=11

$${}_n P_r = \frac{n!}{(n-r)!}$$

${}_n P_r$ = permutation
 n = total number of objects
 r = number of objects selected

overall non-attacking queens = $8 \times 7 = 56$.
 For pair concept = $56 / 2 = 28$

Selection (fitness function) and Crossover

[2, 4, 7, 4, 8, 5, 5, 2]	24
[3, 2, 7, 5, 2, 4, 1, 1]	23
[1, 5, 7, 2, 6, 1, 3, 5]	22
[6, 3, 6, 5, 2, 4, 6, 7]	21
[2, 1, 3, 3, 7, 0, 3, 3]	21
[1, 0, 1, 0, 7, 4, 2, 6]	21
[2, 4, 4, 1, 5, 1, 2, 4]	20
[0, 7, 3, 6, 0, 6, 2, 6]	20
[0, 3, 5, 1, 4, 3, 2, 2]	20
<hr style="border-top: 2px dashed black;"/>	
[0, 7, 2, 3, 0, 1, 2, 5]	19
[5, 1, 1, 3, 3, 4, 5, 3]	19
[6, 5, 0, 5, 3, 3, 0, 5]	18
[0, 2, 2, 3, 5, 1, 0, 1]	18
[4, 2, 7, 3, 4, 4, 7, 3]	18
[2, 3, 6, 3, 0, 5, 2, 5]	17



[2, 4, 7, 4, 8, 5, 5, 2]
[3, 2, 7, 5, 2, 4, 1, 1]
[1, 5, 7, 2, 6, 1, 3, 5]
[6, 3, 6, 5, 2, 4, 6, 7]
[2, 1, 3, 3, 7, 0, 3, 3]
[1, 0, 1, 0, 7, 4, 2, 6]
[2, 4, 4, 1, 5, 1, 2, 4]
[0, 7, 3, 6, 0, 6, 2, 6]
[0, 3, 5, 1, 4, 3, 2, 2]



[2, 4, 7, 4, 2, 4, 1, 1]

[1, 5, 7, 2, 2, 4, 6, 7]

[2, 1, 3, 3, 7, 4, 2, 6]

Mutation , Elitism & Culling

[2, 4, 7, 4, 2, 4, 1, 1]

[2, 4, 7, 4, 2, **5**, 1, 1]

[1, 5, 7, 2, 2, 4, 6, 7]

[1, 5, 7, 2, 2, 4, 6, 7]

[2, 1, 3, 3, 7, 4, 2, 6]

[2, 1, **4**, 3, 7, 4, 2, 6]

[2, 4, 7, 4, 8, 5, 5, 2]	24
[3, 2, 7, 5, 2, 4, 1, 1]	23
[1, 5, 7, 2, 6, 1, 3, 5]	22

Elitism: guarantees that overall fitness will never decrease over time

Culling: individuals below a given threshold are discarded, can lead to a speedup

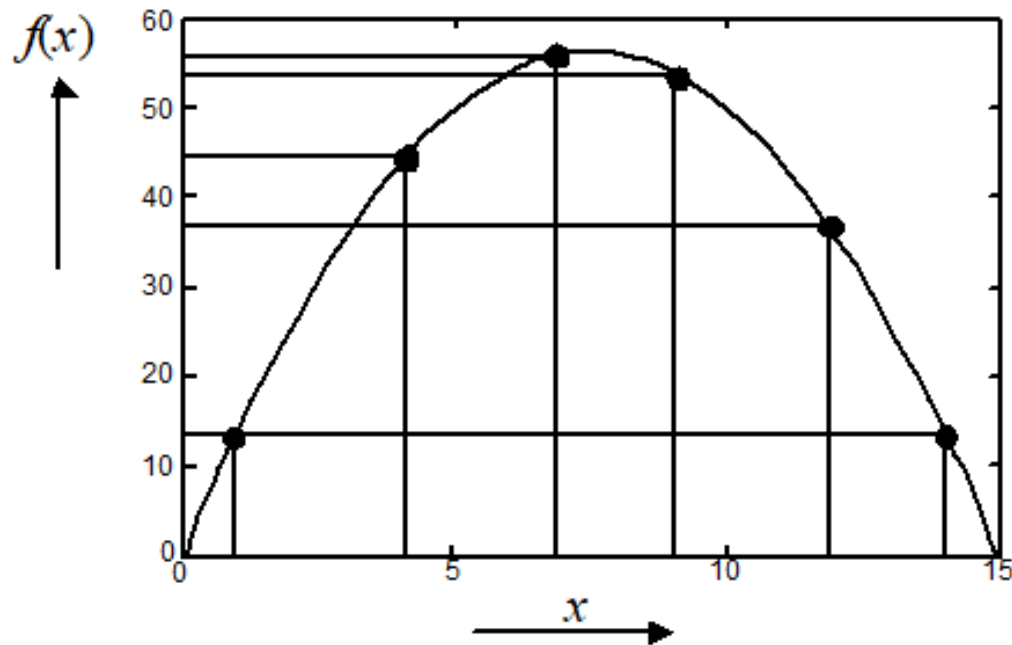
Genetic algorithm

function GENETIC-ALGORITHM(*population, fitness*) **returns** an individual
repeat
 weights \leftarrow WEIGHTED-BY(*population, fitness*)
 population2 \leftarrow empty list
 for *i* = 1 **to** SIZE(*population*) **do**
 parent1, parent2 \leftarrow WEIGHTED-RANDOM-CHOICES(*population, weights, 2*)
 child \leftarrow REPRODUCE(*parent1, parent2*)
 if (small random probability) **then** *child* \leftarrow MUTATE(*child*)
 add *child* to *population2*
 population \leftarrow *population2*
until some individual is fit enough, or enough time has elapsed
return the best individual in *population*, according to *fitness*

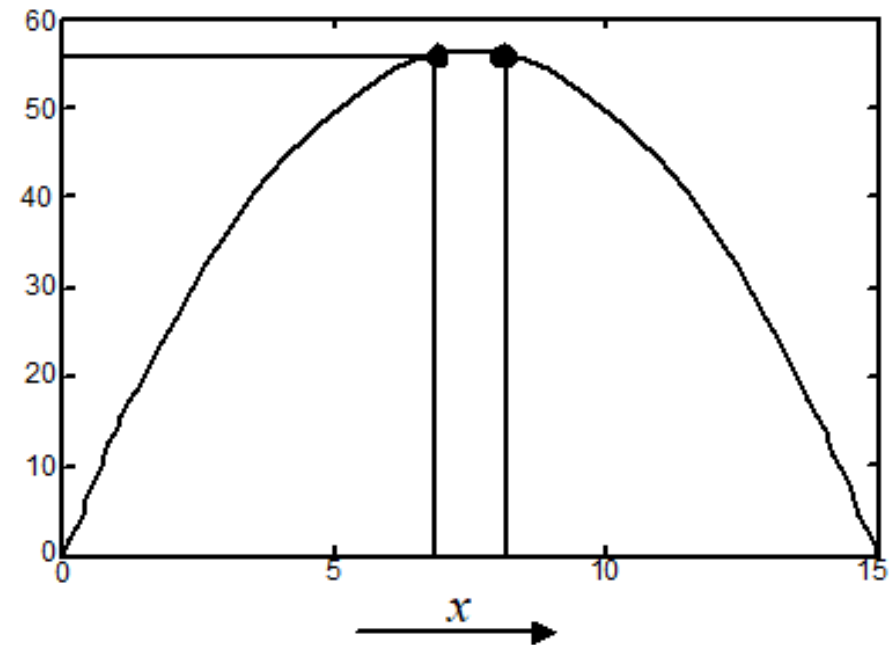
function REPRODUCE(*parent1, parent2*) **returns** an individual
 n \leftarrow LENGTH(*parent1*)
 c \leftarrow random number from 1 to *n*
 return APPEND(SUBSTRING(*parent1, 1, c*), SUBSTRING(*parent2, c + 1, n*))

Genetic algorithms: case study

find the maximum value of the function $(15x - x^2)$ where parameter x varies between 0 and 15



(a) Chromosome initial locations.



(b) Chromosome final locations.

String Representation

chromosomes

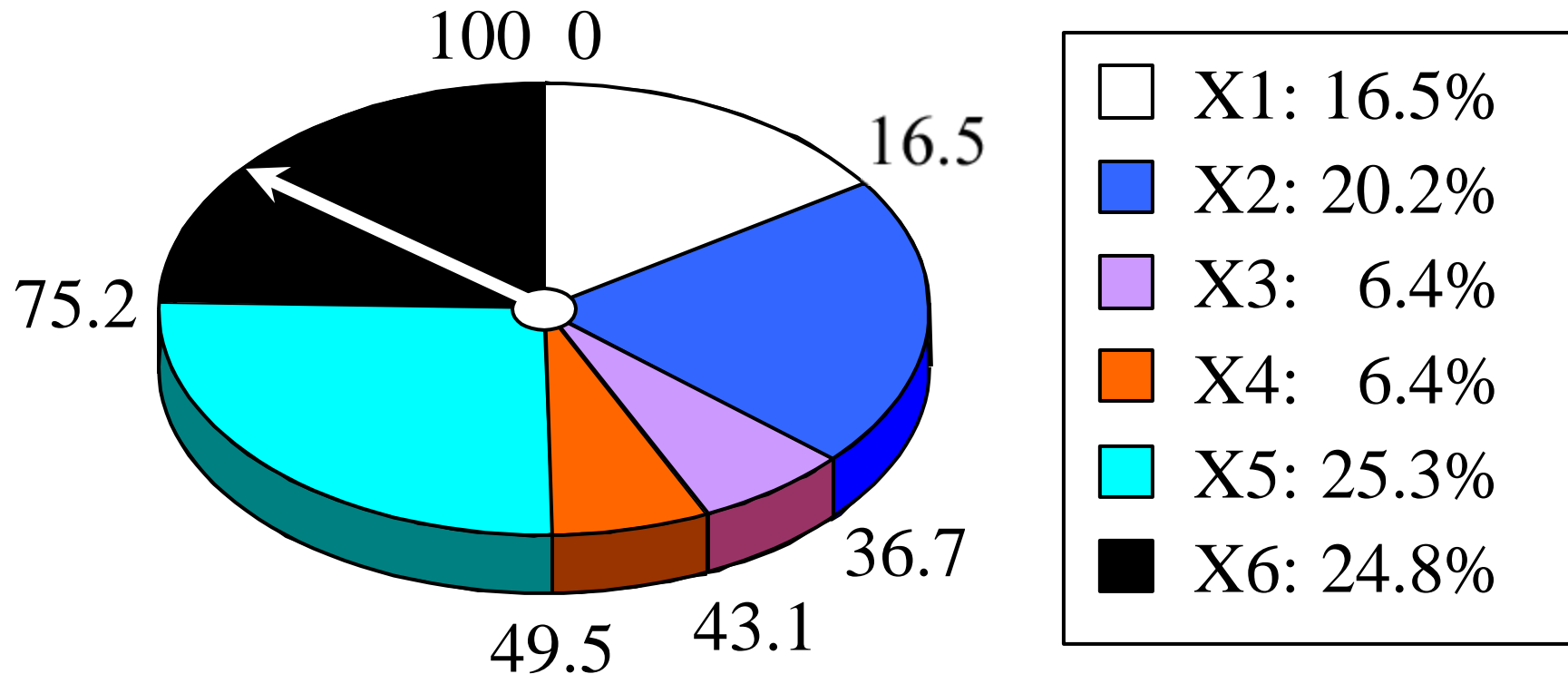
<i>Integer</i>	<i>Binary code</i>	<i>Integer</i>	<i>Binary code</i>	<i>Integer</i>	<i>Binary code</i>
1	0 0 0 1	6	0 1 1 0	11	1 0 1 1
2	0 0 1 0	7	0 1 1 1	12	1 1 0 0
3	0 0 1 1	8	1 0 0 0	13	1 1 0 1
4	0 1 0 0	9	1 0 0 1	14	1 1 1 0
5	0 1 0 1	10	1 0 1 0	15	1 1 1 1

Random Selection

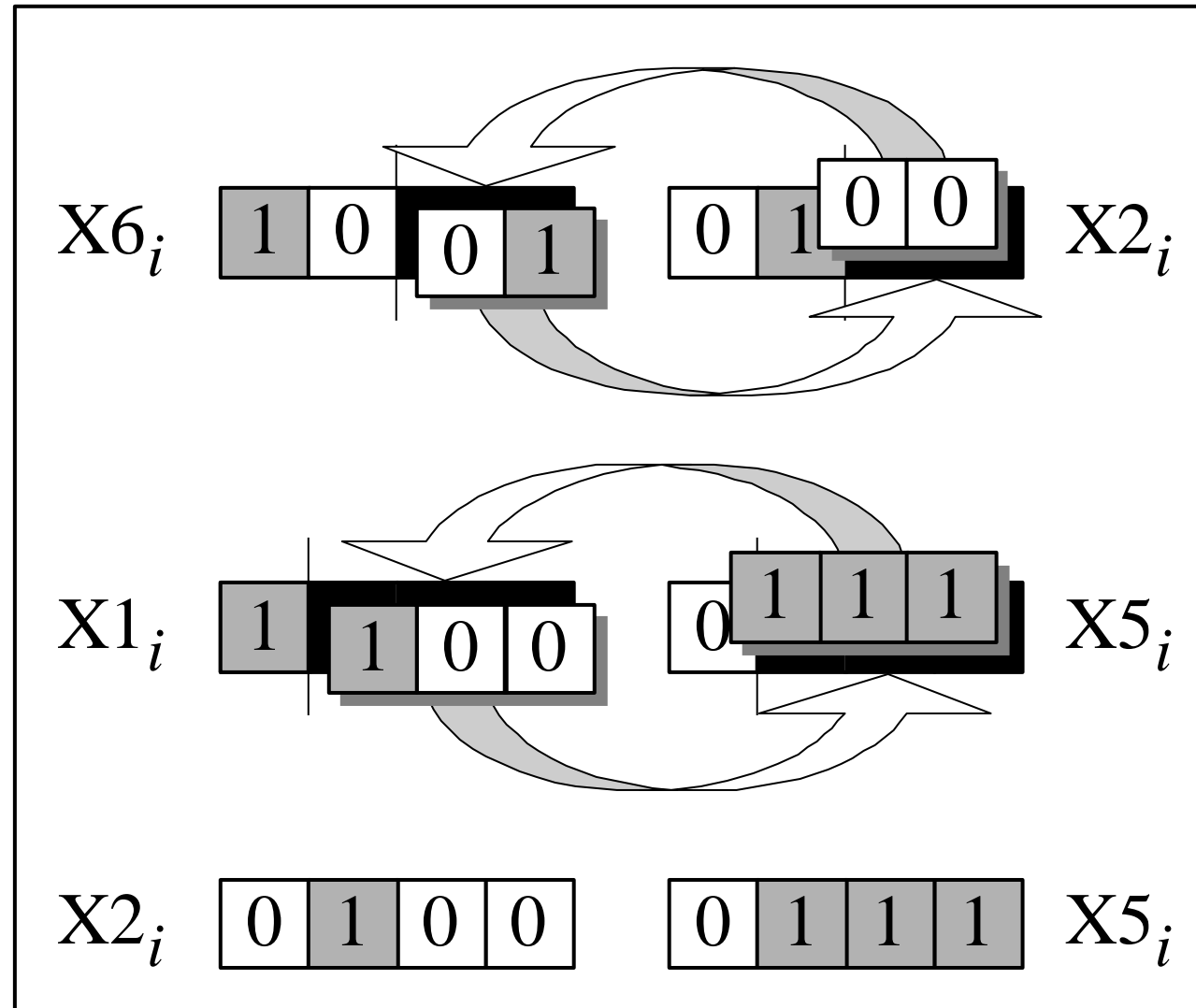
<i>Chromosome label</i>	<i>Chromosome string</i>	<i>Decoded integer</i>	<i>Chromosome fitness $f(x)$</i>	<i>Fitness ratio, %</i> $= \frac{f(x)}{\sum f(x)}$
X1	1 1 0 0	12	36	16.5
X2	0 1 0 0	4	44	20.2
X3	0 0 0 1	1	14	6.4
X4	1 1 1 0	14	14	6.4
X5	0 1 1 1	7	56	25.7
X6	1 0 0 1	9	54	24.8

Roulette wheel selection

The most commonly used chromosome selection techniques is the **roulette wheel selection**.



Crossover



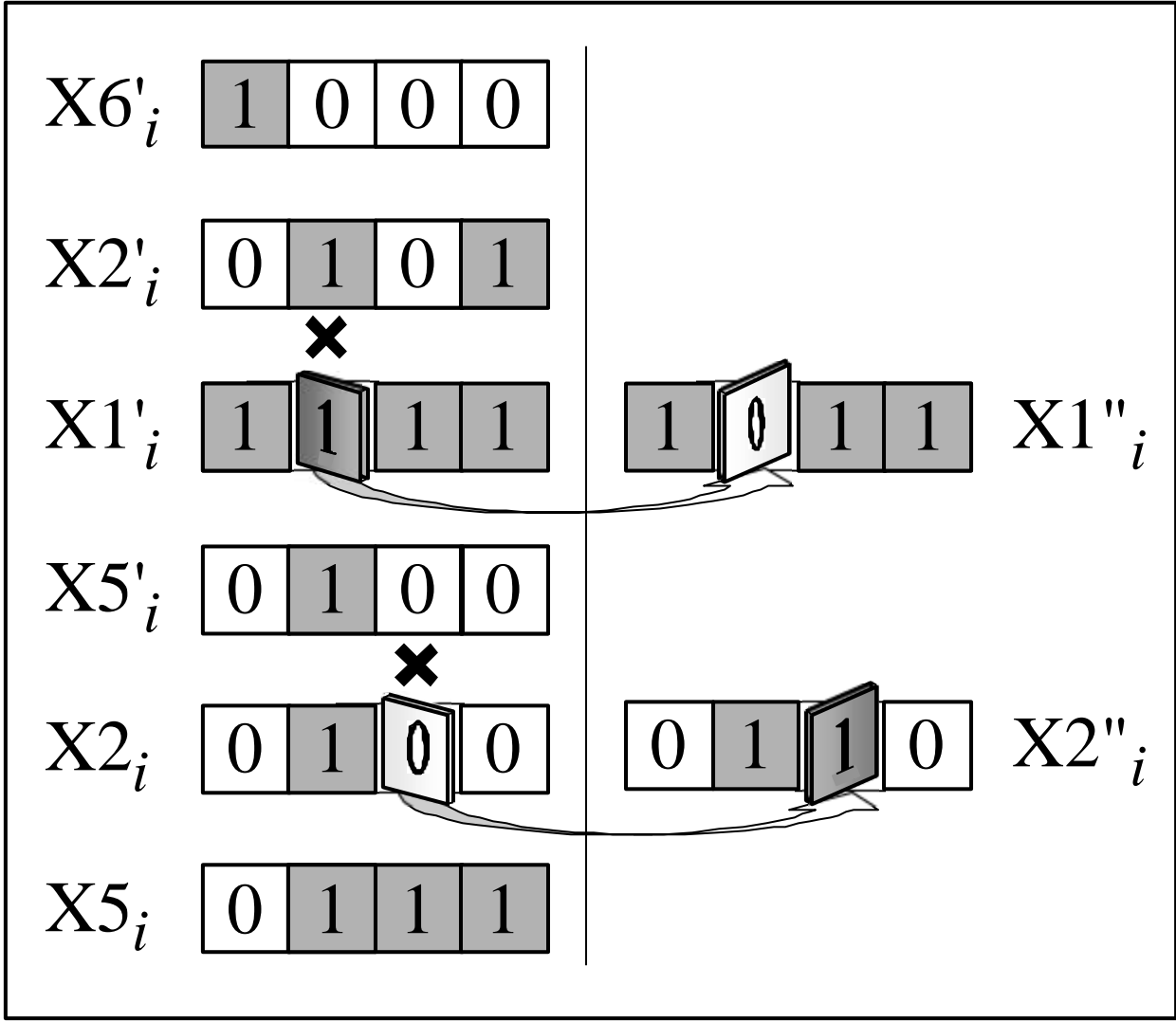
Splitting point
randomly

Elitism

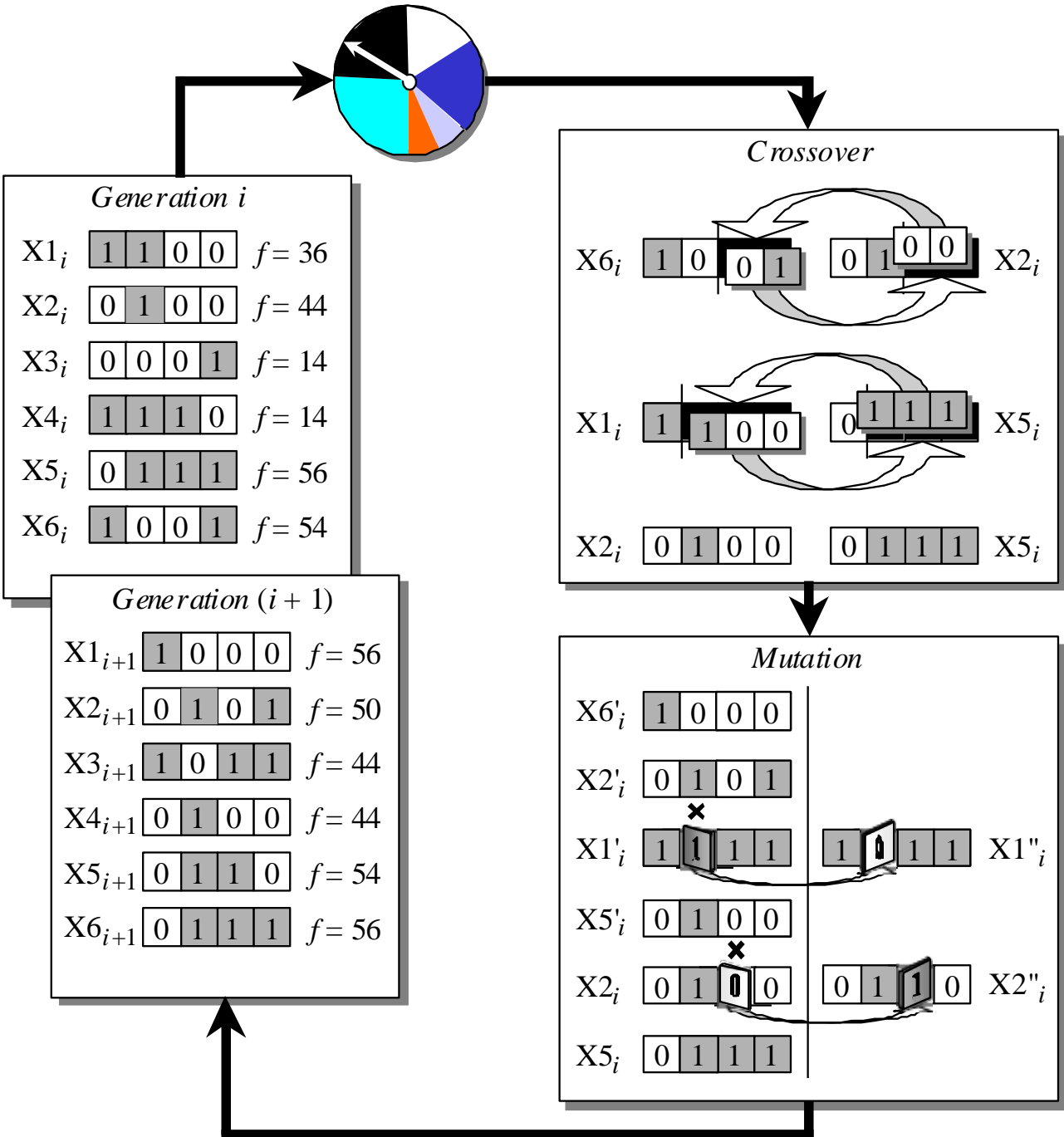
Mutation operator

- Mutation represents a change in the gene.
- Mutation is a background operator. Its role is to provide a guarantee that the search algorithm is not trapped on a local optimum.
- The mutation operator flips a randomly selected gene in a chromosome.
- The mutation probability is quite small in nature, and is kept low for GAs, typically in the range between 0.001 and 0.01.

Mutation



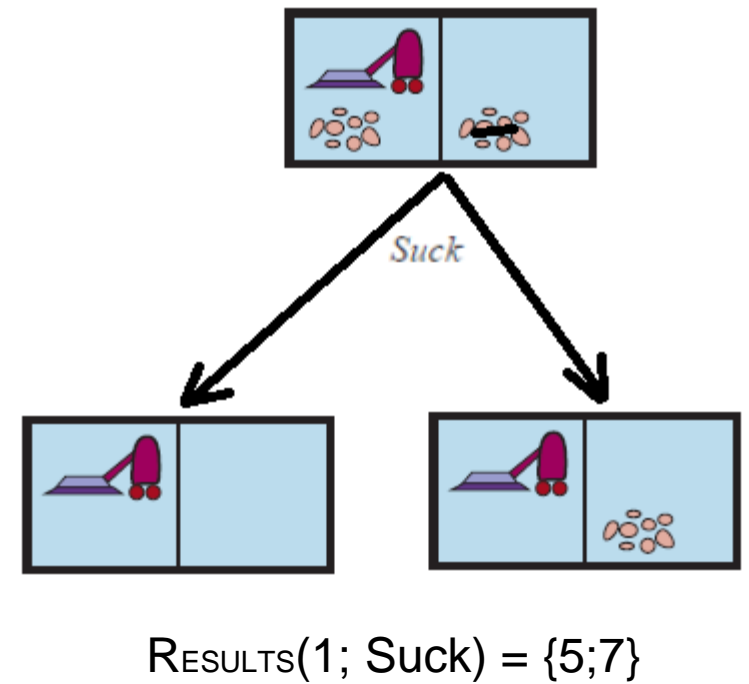
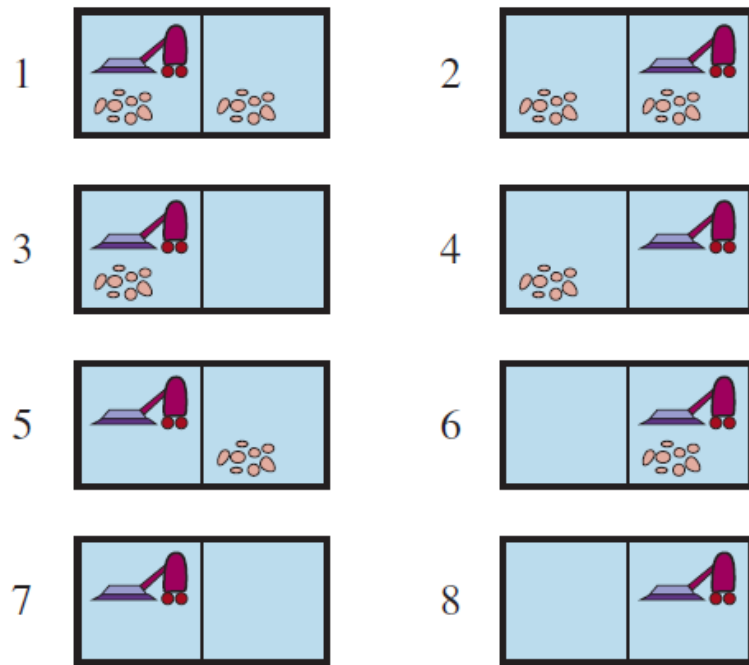
The genetic algorithm cycle



Search with Nondeterministic Actions

Definition

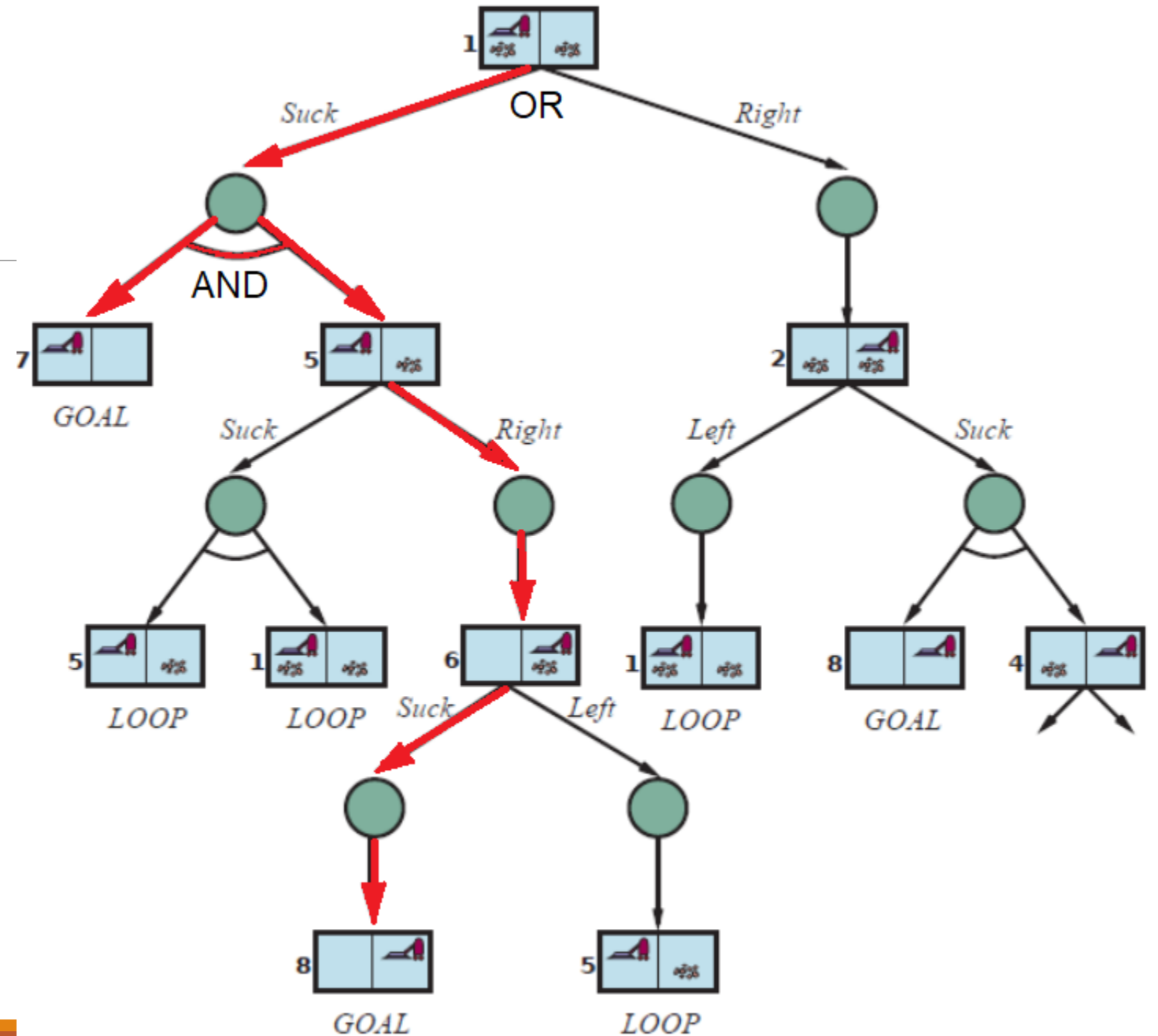
Environment is nondeterministic, the agent doesn't know what state it transitions to after taking an action



AND-OR search trees

In a nondeterministic environment, branching is also introduced by the *environment's choice* of outcome for each action (AND node)

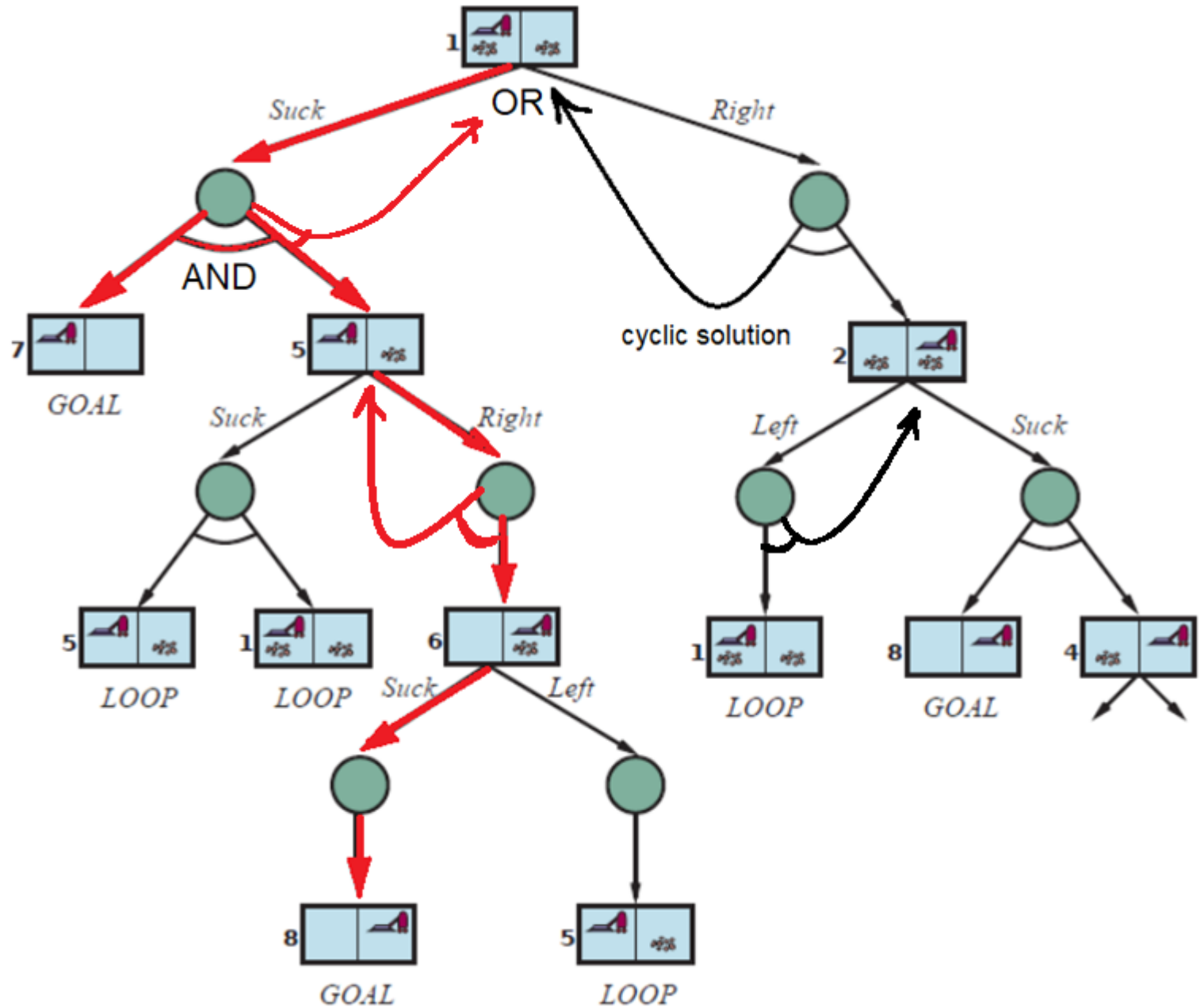
In a deterministic environment, the only branching is introduced by the *agent's own choices* in each state: (OR node)



Looping

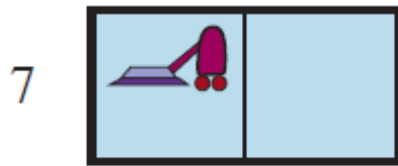
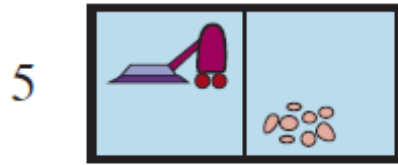
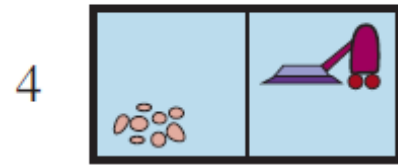
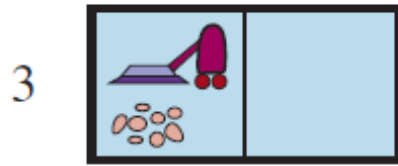
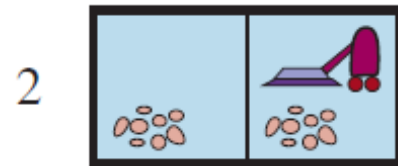
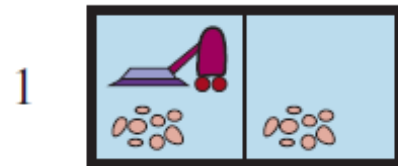
cyclic solution : to keep trying
Action until it works

[while State=1 do Right;Suck]



Search in Partially Observable Environments

known environment , unknown location



No observation at all.

Imagine the light is down in home !! What u have to do ?

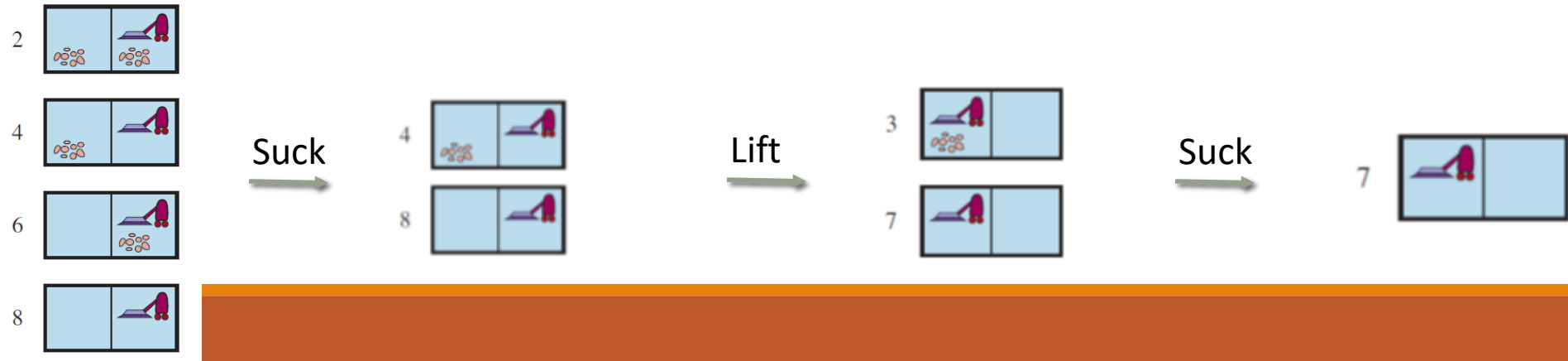
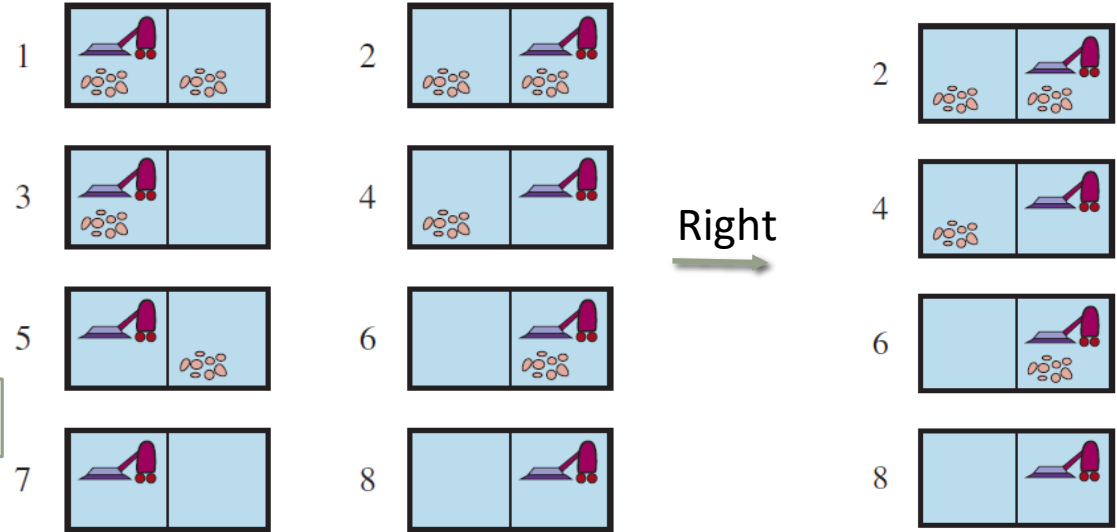
Initial state ?(may be known or not!)

known environment , unknown location

Initial state ?(may be known or not!) but it is limited to state space

Actions : 1- based on current state

$$\text{ACTIONS}(b) = \bigcup_{s \in b} \text{ACTIONS}_P(s).$$



known environment , unknown location

Imagine the light is down in home !! What u have to do ?

Initial state ?(may be known or not!) but it is limited to state space

Actions : 1- based on current state

$$\text{ACTIONS}(b) = \bigcup_{s \in b} \text{ACTIONS}_P(s).$$

Actions : 2- based on current state (some actions are unsafe) →

Limited to safe actions.



Complete solution for vacuum world

