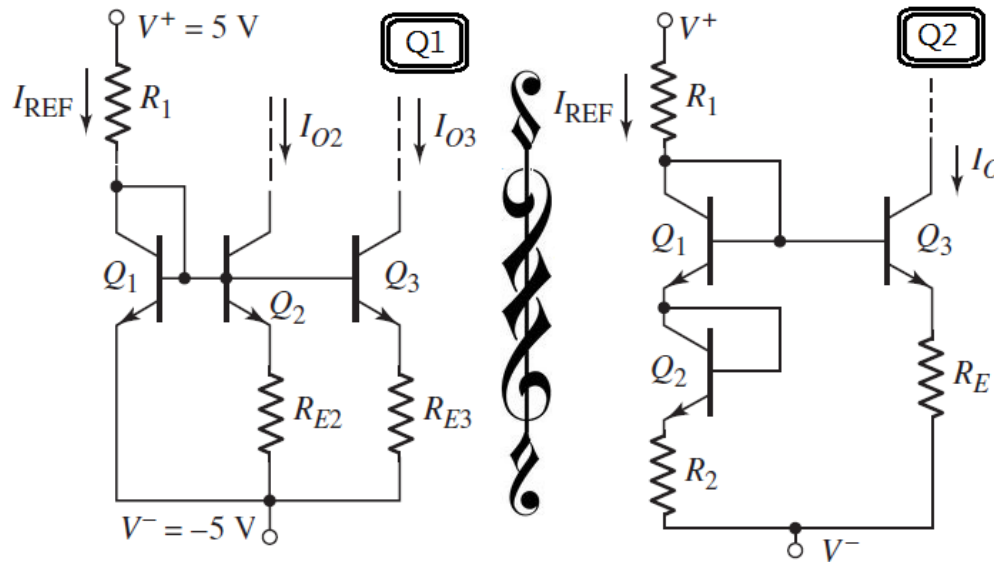




**ANSWER THE FOLLOWING QUESTIONS:**

1. Consider the Widlar current-source circuit with multiple output transistors shown in next Figure. Assume  $V_{BE1} = 0.7V$ . [5 marks] [ $A_q, C_a$ ]
- (a) For circuit parameters  $R_1 = 10k\Omega$ ,  $R_{E2} = 1k\Omega$ , and  $R_{E3} = 2k\Omega$ , find  $I_{REF}$ ,  $I_{O2}$ , and  $I_{O3}$ .
- (b) Determine new values of  $R_{E2}$  and  $R_{E3}$  such that  $I_{O2} = 20\mu A$  and  $I_{O3} = 80\mu A$ .



**Solution:**

(a)

$$I_{REF} = \frac{V^+ + V^- - V_{BE1}}{R_1} = 390\mu A$$

$$V_{BE1} = V_{BE2} + I_{E2}R_{E2}$$

$$I_{E2} = \frac{\beta I_{O2}}{(\beta + 1)}$$

$$\frac{\beta I_{O2}}{(\beta + 1)} R_{E2} = V_T \ln \left( \frac{I_{REF}}{I_{O2}} \right)$$

$$38.5K I_{O2} = \ln \left( \frac{0.39m}{I_{O2}} \right)$$

$$38.5K I_{O2} + \ln I_{O2} = -7.8 \Rightarrow I_{O2} \cong 190\mu A$$

(b)

$$R_{E2} = V_T \ln \left( \frac{I_{REF}}{I_{O2}} \right) \times \frac{(\beta + 1)}{\beta I_{O2}} = 9.95K\Omega$$

$$R_{E3} = V_T \ln \left( \frac{I_{REF}}{I_{O3}} \right) \times \frac{(\beta + 1)}{\beta I_{O2}} = 2.03K\Omega$$

[Total Marks is 10]

2. Assume that all transistors in the circuit in previous Figure are matched and that  $\beta = \infty$  (neglect base currents). [5 marks] [A<sub>p</sub>,B<sub>i</sub>]

- (a) Derive an expression for  $I_O$  in terms of bias voltages and resistor values.  
 (b) For  $V^+ = +5V$  and  $V^- = -5V$ , design the circuit such that  $I_O = 0.5 \text{ mA}$ .  
 (c) Expand the current source circuit to supply  $2I_O$ .

**Solution:**

(a)

$$I_{REF} = \frac{V^+ + V^- - 2V_{BE1}}{R_1 + R_2} \quad (1)$$

$$V_B = V_{BE1} + V_{BE1} + I_{REF}R_2 = V_{BE3} + I_O R_E \quad \text{tran. matched}$$

$$V_{BE} + I_{REF}R_2 = I_O R_E$$

$$V_T \ln \left( \frac{I_{REF}}{I_S} \right) + I_{REF}R_2 = I_O R_E$$

$$I_O = \frac{V_T}{R_E} \ln \left( \frac{I_{REF}}{I_S} \right) + \frac{R_2}{R_E} I_{REF}$$

(b) To simplify the solution since there are many variables, there are some assumptions will be made: assume  $V_{BE} = 0.7V$ ,  $R_1 = R_2$ ,  $I_{REF} = I_O$

$$V_{BE} + I_{REF}R_2 = I_O R_E$$

$$V_{BE} + I_O R_2 = I_O R_E \Rightarrow R_E = R_2 + 1.4K$$

$$I_{REF} = \frac{V^+ + V^- - 2V_{BE1}}{R_1 + R_2} \Rightarrow R_2 = \frac{V^+ + V^- - 2V_{BE1}}{2I_O} = 8.6K\Omega \Rightarrow R_E = 10K\Omega$$

