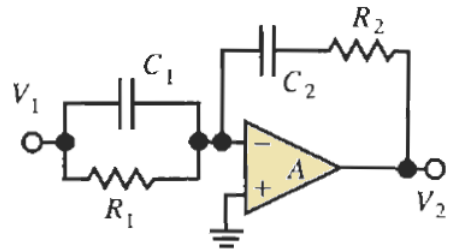




ANSWER THE FOLLOWING QUESTIONS:

1. Consider the inverting Op Amp circuit in the next figure. [15 marks] [A_o, C_p]
- Drive an expression for the characteristic equation. Define the function of this circuit.
 - Briefly, discuss the effects of the pole locations.
 - Reconnect C_2 to be shunted across R_2 . Drive an expression for the new structure.[Hint: arrange the equation in form to be drawn by bode plot]
 - Calculate the component values to realize a zero at $f_z = 830Hz$, pole at $f_p = 2kHz$, and a high frequency gain of $6.36dB$. [Hint: $C_1 = 50nF$]
 - Draw the bode plot of the characteristic equation of the previous item.



Solution: Q1.(a)

$$Z_F = \frac{1}{SC_2} + R_2 = \frac{SR_2C_2 + 1}{SC_2}$$

$$Z_i = \frac{\frac{1}{SC_1}R_1}{\frac{1}{SC_1} + R_1} = \frac{R_1}{SC_1R_1 + 1}$$

$$\text{inverting Op Amp gain} = -\frac{Z_F}{Z_i}$$

$$\therefore \frac{V_o}{V_i} = \frac{\frac{SC_2 + R_2}{R_1}}{\frac{SC_1R_1 + 1}{SC_2R_1}} = \frac{(SR_2C_2 + 1)(SC_1R_1 + 1)}{SC_2R_1}$$

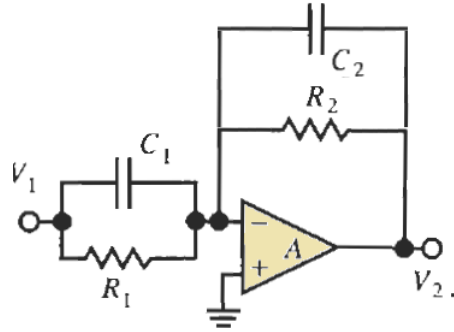
(b) The characteristic equation of previous circuit will be affected by poles location since we have two poles @ $0, \infty$.

these poles will imply infinite gain at the origin and at infinity.

at $\omega = 0 \Rightarrow C_2 = \text{open circuit}$. The Op Amp will operate in open loop.

at $\omega = \infty \Rightarrow C_1 = \text{short circuit}$. The Op Amp gain will be infinity.

(c)



$$Z_F = \frac{\frac{1}{SC_2} R_2}{\frac{1}{SC_2} + R_2} = \frac{R_2}{SC_2 R_2 + 1}$$

$$Z_i = \frac{\frac{1}{SC_1} R_1}{\frac{1}{SC_1} + R_1} = \frac{R_1}{SC_1 R_1 + 1}$$

$$\text{inverting Op Amp gain} = -\frac{Z_F}{Z_i}$$

$$\therefore \frac{V_o}{V_i} = -\frac{R_2 (SC_1 R_1 + 1)}{R_1 (SR_2 C_2 + 1)}$$

(d)

$$K = 23 = 20 \log \left(\frac{R_2}{R_1} \right) \Rightarrow \frac{R_2}{R_1} = 10^{6.36/20} = 2.08$$

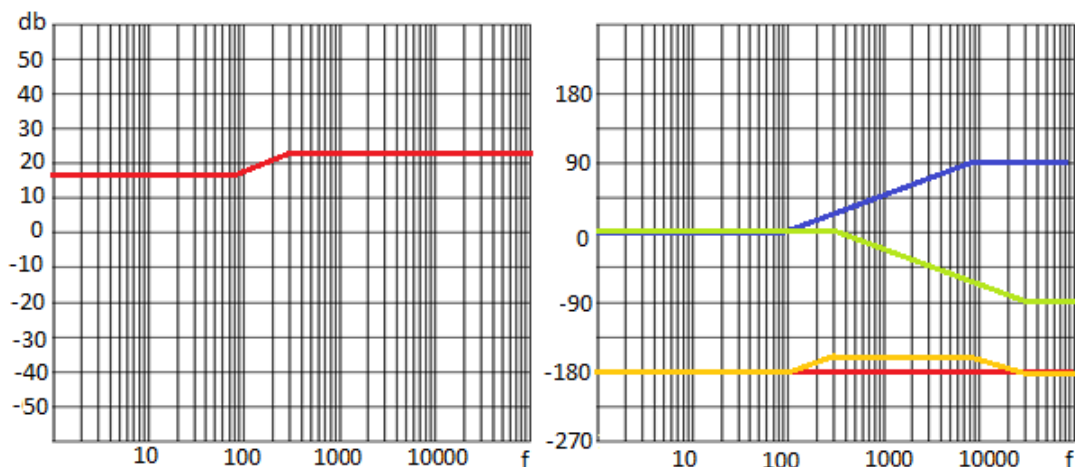
$$\text{zero at } 830\text{Hz} \Rightarrow \omega_z = \frac{1}{C_1 R_1} = 2\pi \times 830 = 5212.4$$

$$\text{assume } C_1 = 50\text{nF} \Rightarrow R_1 = 3.84\text{k}\Omega$$

$$\therefore R_2 = 2.08 R_1 = 7.98\text{k} \approx 8\text{k}\Omega$$

$$\text{pole at } 2\text{K} \Rightarrow \omega_p = \frac{1}{C_2 R_2} = 2\pi \times 2\text{k} = 12560 \Rightarrow C_2 \approx 10\text{nF}$$

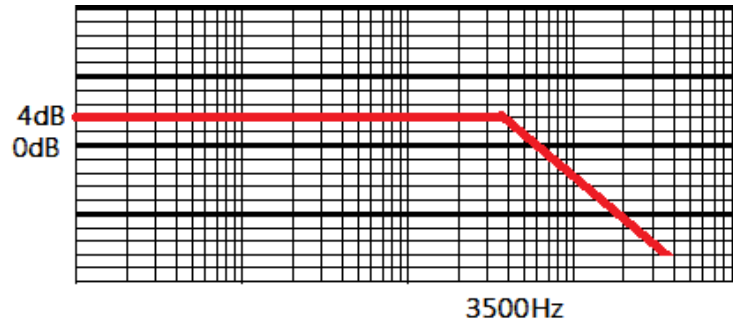
(e)



2. Consider the magnitude plot in the next figure.

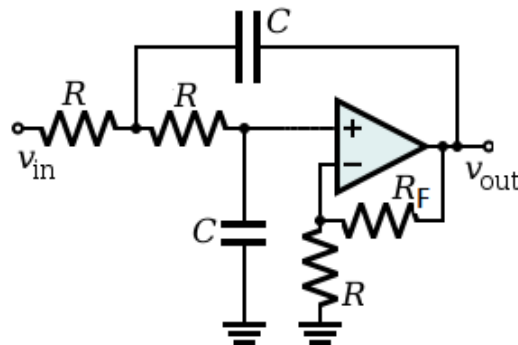
[15 marks] [B_a, A_d, A_q]

- Find the Sallen Key circuit that will realize the given specifications. Find the proper values of the circuit components.
- Calculate the error percentage of Q if the R_F increased 10%.
- Design Band pass Filter (1250 to 3500 Hz). Draw the circuit.



Solution: (a)

- From the figure $Q=0.707 \Rightarrow gain = 3 - \frac{1}{Q} = 1.58$
- Assume $C=0.01\mu F \Rightarrow R = \frac{1}{2\pi \times 3500 \times 0.01\mu} = 4.5k\Omega$
- $R_F = 0.58R = 0.58 \times 4.5 = 2.6K\Omega$



(b)

- Error percentage in gain $k = 1 + \frac{1.1R_F}{R} = 1 + 1.1 \times 0.58 = 1.638 \Rightarrow \Delta K = \frac{1.638}{1.58} = 1.036$
- $Q = \Delta K Q = 1.036 \times 0.707 = 0.733$

(c)

- For HPF: $Q=0.707 \Rightarrow gain = 3 - \frac{1}{Q} = 1.58$

- Assume $C=0.01\mu\text{F} \Rightarrow R = \frac{1}{2\pi \times 1250 \times 0.01\mu} = 1.273\text{k}\Omega$
- $R_F = 0.58R = 0.58 \times 4.5 = 746\text{K}\Omega$
- For the LPF: use the same values.

